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**UTILITY PATENT APPLICATION TRANSMITTAL**  
**(Large Entity)**

(Only for new nonprovisional applications under 37 CFR 1.53(b))

Docket No.  
13414 (NECI1083)

Total Pages in this Submission

**TO THE ASSISTANT COMMISSIONER FOR PATENTS**Box Patent Application  
Washington, D.C. 20231

Transmitted herewith for filing under 35 U.S.C. 111(a) and 37 C.F.R. 1.53(b) is a new utility patent application for an invention entitled:

**METHOD FOR MATCHING A TWO DIMENSIONAL IMAGE TO ONE OF A PLURALITY OF THREE DIMENSIONAL CANDIDATE MODELS CONTAINED IN A DATABASE**

and invented by:

A. Peter Blicher, et al.

jc678 U.S. PTO  
09/538209  
03/30/00If a **CONTINUATION APPLICATION**, check appropriate box and supply the requisite information:☐ Continuation ☐ Divisional ☐ Continuation-in-part (CIP) of prior application No.: \_\_\_\_\_

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Enclosed are:

**Application Elements**

1. ☒ Filing fee as calculated and transmitted as described below
2. ☒ Specification having 52 pages and including the following:
  - a. ☒ Descriptive Title of the Invention
  - b. ☐ Cross References to Related Applications (if applicable)
  - c. ☐ Statement Regarding Federally-sponsored Research/Development (if applicable)
  - d. ☐ Reference to Microfiche Appendix (if applicable)
  - e. ☒ Background of the Invention
  - f. ☒ Brief Summary of the Invention
  - g. ☒ Brief Description of the Drawings (if drawings filed)
  - h. ☒ Detailed Description
  - i. ☒ Claim(s) as Classified Below
  - j. ☒ Abstract of the Disclosure

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**Application Elements (Continued)**

3. ☒ Drawing(s) *(when necessary as prescribed by 35 USC 113)*
- a. ☒ Formal                      Number of Sheets 3
- b. ☐ Informal                      Number of Sheets \_\_\_\_\_
4. ☒ Oath or Declaration
- a. ☒ Newly executed *(original or copy)*      ☐ Unexecuted
- b. ☐ Copy from a prior application (37 CFR 1.63(d)) *(for continuation/divisional application only)*
- c. ☒ With Power of Attorney      ☐ Without Power of Attorney
- d. ☐ DELETION OF INVENTOR(S)  
Signed statement attached deleting inventor(s) named in the prior application,  
see 37 C.F.R. 1.63(d)(2) and 1.33(b).
5. ☐ Incorporation By Reference *(usable if Box 4b is checked)*  
The entire disclosure of the prior application, from which a copy of the oath or declaration is supplied  
under Box 4b, is considered as being part of the disclosure of the accompanying application and is hereby  
incorporated by reference therein.
6. ☐ Computer Program in Microfiche *(Appendix)*
7. ☐ Nucleotide and/or Amino Acid Sequence Submission *(if applicable, all must be included)*
- a. ☐ Paper Copy
- b. ☐ Computer Readable Copy *(identical to computer copy)*
- c. ☐ Statement Verifying Identical Paper and Computer Readable Copy

**Accompanying Application Parts**

8. ☒ Assignment Papers *(cover sheet & document(s))*
9. ☐ 37 CFR 3.73(B) Statement *(when there is an assignee)*
10. ☐ English Translation Document *(if applicable)*
11. ☐ Information Disclosure Statement/PTO-1449      ☐ Copies of IDS Citations
12. ☐ Preliminary Amendment
13. ☒ Acknowledgment postcard
14. ☒ Certificate of Mailing
- ☐ First Class      ☒ Express Mail *(Specify Label No.):* EL357933440US

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**Accompanying Application Parts (Continued)**

15. ☐ Certified Copy of Priority Document(s) *(if foreign priority is claimed)*

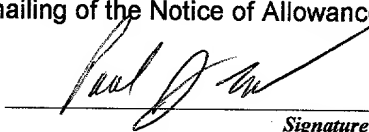
16. ☐ Additional Enclosures *(please identify below):*

**Fee Calculation and Transmittal**

**CLAIMS AS FILED**

For	#Filed	#Allowed	#Extra		Rate	Fee
Total Claims	28	- 20 =	8	x	\$18.00	\$144.00
Indep. Claims	12	- 3 =	9	x	\$78.00	\$702.00
Multiple Dependent Claims (check if applicable) <input type="checkbox"/>						\$0.00
BASIC FEE						\$690.00
OTHER FEE (specify purpose) <u>Assignment</u>						\$40.00
TOTAL FILING FEE						\$1,576.00

- ☒ A check in the amount of \$1,576.00 to cover the filing fee is enclosed.
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- ☐ Charge the issue fee set in 37 C.F.R. 1.18 at the mailing of the Notice of Allowance, pursuant to 37 C.F.R. 1.311(b).

  
Signature

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cc:

METHOD FOR MATCHING A TWO DIMENSIONAL IMAGE TO ONE OF A PLURALITY  
OF THREE DIMENSIONAL CANDIDATE MODELS CONTAINED IN A DATABASE

## BACKGROUND OF THE INVENTION

## 1. Field of the Invention

This invention relates generally to computer vision and more particularly to the recognition and identification of a face or other object from among a stored database of three dimensional (3D) models when presented with an arbitrary two dimensional (2D) photograph of a face or object, under arbitrary pose and lighting conditions.

## 2. Prior Art

There are two subfields of computer vision that are closely related to the field of this invention: face recognition, and object recognition. Face recognition has primarily been concerned with identifying 2D images of human faces, or matching 2D images of faces to other such 2D images. The methods of the prior art have not used 3D models of faces to identify 2D images.

The field of object recognition, however, has had a major concern with identifying 2D images based on known 3D models. There have been numerous works in this area. A more recent example is the methods that use what is called "alignment".

The usual methods consist of extracting some features from the gray scale image which are then matched with candidate features from the models. Examples of features are special points (such as corners), extracted edges, configurations of edges (such as parallel edges, sometimes referred to as "ribbons"), etc. The primary problems in the object recognition literature revolve

around how to (1) choose good features, (2) how to manage the combinatorial explosion that results from the possibilities of matching large numbers of image features with large numbers of model features, and (3) how to measure the quality of a match in the presence of numerous sources of error. The issue of lighting enters primarily at the (early) stage when features for matching are being extracted. The prior art related to object recognition has considerable bearing on performing step (1) above (pose estimation), but has little to say about the problem of accounting for the effects of light that are needed in steps (2) and (3).

Face recognition, on the other hand, has had considerable interest in dealing with lighting. The face recognition literature has evolved a number of methods of dealing with variations in lighting. These revolve around two main approaches: (1) estimating the lighting conditions (as in step (2) above), or (2) analyzing the space of images that is created as the lighting is varied. Typically, method (2) takes advantage of "principal components analysis" (PCA) to identify the dimensions of the image space where the most variation occurs. These typically image-based methods have been fairly successful under conditions where pose does not vary. However, in general they have not been concerned with the use of 3D models, although there are those in the art who have constructed 3D models from images, and have been concerned about the relations between images and 3D structure, as have a large fraction of workers in computer vision.

There is also significant work by others in the art on using the space of distortions of a face in conjunction with the observed shading to permit a linearization that in turn admits a PCA analysis on which recognition can be based. These artisans use a method based on distortions of graphs that join standard feature

points on the face or similar methods, which have been applied in commercially available systems. Many groups in recent years have been interested in face recognition and the literature that has arisen in the past 5 or so years is quite large. The primary focus of all these methods, however, has been on identifying 2D images based on training sets of other 2D images.

A major contributing factor to the explosion in interest in face recognition was the successful application of PCA methods to the problem. This was impressive because it was a tractable solution to what had hitherto been considered an intractable problem. However, there are severe limitations with respect to variation of the conditions under which the data must be captured; in particular, lighting, pose, and scale must be as constant as possible. These limitations can be traced to the fact that PCA is a linear decomposition and therefore only will give good results when the space it is being applied to is a linear space. The space of images under varying pose is not linear, and therefore PCA breaks down. Those in the art have addressed this problem by finding particular ways to convert the nonlinear space back to a linear one that is amenable to PCA. Still others in the art have pointed out that in the simplest cases, any image of such a simple object was just a linear combination of the images under almost any 3 different lighting conditions. This led to activity in this area, culminating with work on rigorously working out the relationship between lighting and the space of images. It should be pointed out, however, that in the presence of shadows, the situation is still quite complex.

There are apparatus known in the art for capturing 3D models of people's faces. These apparatus capture pictures of the faces in registration with the 3D models that are captured. The 3D models consist of the 3-dimensional coordinates of a large number of points on the surface of the face, typically on the order of 640

x 640, along with the color picture value at each point. This provides the possibility of realistic computer graphics rendering of the faces from any vantage point.

5 It is envisioned that these apparatus can be used to capture a large number of face models. In some applications, this number could reach on the order of one million faces or more.

10 One application of such apparatus is face identification, i.e., given a query consisting of an arbitrary 2D photograph of a face, to search a large database of previously captured 3D models of faces to find the model which best matches the photograph.

15 There are numerous obstacles to be overcome to accomplish this. In general, there is no knowledge or control of the conditions under which the query photograph was acquired. Therefore, the pose (i.e. the position and orientation of the subject) and the lighting conditions of the query photograph are unknown.

20 One prior art paradigm, in this setting, for matching a query to a model, proceeds as follows:

25 1) the pose of the face in the query is determined. For purposes of this application, "pose" is defined as the 3D position and orientation of the face;

30 2) the lighting in the query is determined. This means finding the direction, intensity, and color of any number of light sources which may have been illuminating the subject when the query photograph was acquired;

3) for each model in the database, computer graphics techniques are then used to render a realistic image of the model in the pose and lighting conditions determined in steps (1) and (2); and

4) among the renderings computed in the previous step, the one which most closely approximates the query is found.

5 All of these steps involve difficulties which the current state of the art has not overcome. The methods of the present invention concerns the second, third and fourth steps, namely, finding the lighting conditions in the query, and determining which proposed candidate would appear most like the query under those lighting conditions.

The impediment in the method of the prior art described above is that to solve for lighting requires knowing the 3-dimensional configuration of the surface that was photographed, as well as its reflectance characteristics. However, the query does not provide any of this information directly. A large effort in computer vision over the past 40 years has been devoted to inferring this information from one or more pictures.

The methods of the prior art perform steps (2) and (3) above by first solving for lighting by solving the image irradiance equation (the Lambertian imaging equation), which is a system of linear equations, with 5 independent variables for each potential light source: 2 variables indicating the direction of the light (for example, bearing and azimuth), and 3 variables indicating the red, blue, and green intensity, respectively. The number of equations is equal to the number of data points in the image for which surface normal and reflectance are available times the number of color components, typically 3. However, an important constraint is the requirement that the light intensities must not be negative. This latter requirement precludes solving the system using a standard method for linear systems, and instead requires a more sophisticated method, such as a linear programming technique, or the algorithm known as nonnegative



least squares. These special techniques require significantly greater computer time to solve than the same system would require without the constraints of non-negativity. This approach was brought forth by those in the art, as mentioned above.

5

#### SUMMARY OF THE INVENTION

Therefore it is an object of the present invention to provide a method for matching a 2D image to one of a plurality of 3D candidate models contained in a database in which an object is identified without the need for solving for light sources or other complex and costly computations such as eigenvector determination.

It is a further object of the present invention to provide a method for matching a 2D image to one of a plurality of 3D candidate models contained in a database which has relatively lower costs over prior art methods that solve for lighting.

It is yet a further object of the present invention to provide a method for matching a 2D image to one of a plurality of 3D candidate models contained in a database which is simpler than prior methods.

It is still yet a further object of the present invention to provide a method for matching a 2D image to one of a plurality of 3D candidate models contained in a database which does not require iterative algorithms that take one to two orders of magnitude more computer time on the size of problems involved.

Accordingly, a method for matching a two dimensional image to one of a plurality of three dimensional candidate models is provided. The method comprises the steps of: determining the position and orientation of an object giving rise to the two dimensional

image; computing a representation of lighting effects that allows the lighting that gave rise to the two dimensional image to be used to render a realistic image of a three dimensional model; successively rendering each three dimensional candidate model in the determined position and orientation using the surface normals in conjunction with the corresponding computed representation of lighting effects; and comparing the two dimensional image with each of the rendered three dimensional candidate models.

Another method for matching a two dimensional image to one of a plurality of three dimensional candidate models is also provided. This method comprises the steps of: determining the position and orientation of an object giving rise to the two dimensional image; computing a representation of lighting effects based on the plurality of three dimensional candidate models and the two dimensional image that allows evaluation of the likelihood that a particular three dimensional candidate model gave rise to a particular two dimensional image; and choosing the most likely model to have generated the query based on the computed representation of lighting effects.

In a first variation of the methods for matching a two dimensional image to one of a plurality of three dimensional candidate models, the method comprises the steps of: determining the position and orientation of the two dimensional image; for each three dimensional model, computing a histogram-like table having a computed brightness coefficient for each surface normal of the model based on the corresponding value in the two dimensional image, each brightness coefficient depending only on the corresponding surface normal; successively rendering each three dimensional model in the determined position and orientation using the surface normals in conjunction with the corresponding computed brightness histogram-like table; and comparing the two dimensional image with each of the rendered

three dimensional models.

5 In a second variation of the methods for matching a two  
dimensional image to one of a plurality of three dimensional  
candidate models, the method comprises the steps of: determining  
the position and orientation of the two dimensional image; for  
each three dimensional model, computing a histogram-like table  
having a computed brightness coefficient for each surface normal  
of the model based on the corresponding value in the two  
10 dimensional image, each brightness coefficient depending only on  
the corresponding surface normal; computing the variance of the  
brightness coefficients that are used to create each bucket of  
the histogram-like table, a bucket being a set of similar normal  
values that are lumped together to form a single argument value  
in the histogram-like table; computing the sum of the variances  
of the histogram-like table buckets; and ranking the three  
dimensional models using its computed sum as an error function,  
the ranking indicating the likelihood that the corresponding  
three dimensional model matches the two dimensional image.

20 Still further provided is a program storage device readable by  
machine, tangibly embodying a program of instructions executable  
by the machine to perform the method steps of the methods and  
variations thereof of the present invention and a computer  
25 program product embodied in a computer-readable medium for  
carrying out the methods, and variations thereof, of the present  
invention. Preferably, the computer program has modules  
corresponding to the steps of the methods and variations thereof  
of the present invention.

#### 30 BRIEF DESCRIPTION OF THE DRAWINGS

These and other features, aspects, and advantages of the methods  
of the present invention will become better understood with

regard to the following description, appended claims, and accompanying drawings where:

FIG. 1 illustrates a schematical representation of the method of the present invention.

FIG. 2 further illustrates the lightsphere module of FIG. 1.

FIG. 3 illustrates a graphical representation of the lightsphere data structure of FIG. 2.

#### DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENT

Although this invention is applicable to numerous and various types of objects to be recognized, it has been found particularly useful in the environment of human face recognition. Therefore, without limiting the applicability of the invention to human face recognition, the invention will be described in such environment.

The methods of the present invention, have an efficient method of comparing a query photograph, such as a face of a person to be identified to one of a plurality of 3D models contained in a database. The methods of the present invention presupposes a particular model of reflectance, known as the Lambertian assumption. Although the invention is robust against deviations of the true details of reflectance from this model, the relevant point is that this is a functional relationship between the data in the query and the data in the model, i.e., there is an equation that relates the query and the model. The methods of the present invention can be viewed as an efficient way of measuring to what degree the expected form of this functional relationship holds between the query and the putative model from which it arose. This measure can be generalized; for example, the statistical notion of correlation is a generalization of

functional relation.

Another generalization, which arose primarily in information theory, depends on the entropies of the distributions governing the objects we want to compare. These distributions, for example, could govern the point values of different measurements in the two objects. Entropy can be regarded as a measure of uncertainty, i.e., the greater the entropy, the more difficult it is to predict the outcome of drawing a sample from a probability distribution. When we have two random variables with a joint distribution, e.g. the data values of a 3D model and of a 2D image putatively of that model, it can be determined to what extent does knowing the value of one of these random variables, say a 9-point patch on the 3D model, help us predict the value of the other variable, say the intensity at a corresponding pixel in the 2D image. This question is quantified by taking the difference between the entropy of the marginal distribution of the second variable, and subtracting off the entropy of the conditional distribution of the second variable given the first. This yields how much our uncertainty decreased thanks to knowledge of the first variable. This can be summarized by:

$$I(Y;X) = H(Y) - H(X|Y) \quad (1)$$

where  $H$  denotes entropy,  $X$  is the first random variable, and  $Y$  is the second random variable. This quantity, denoted by  $I(Y;X)$  is known as the mutual information between  $X$  and  $Y$ . It is symmetric, and is also equal to

$$H(X) + H(Y) - H(X,Y) \quad (2)$$

where  $H(X,Y)$  is the entropy of the joint distribution of  $X$  and  $Y$ .

Thus, the methods of the present invention can be thought of as a

particular approximation to measuring the mutual information between the (distributions governing the) 3D model and the 2D query.

5 In a system where a 2D photographic query is to be matched to a 3D model in a large database of such models by predicting the appearance of each model under the pose and lighting conditions that created the query, the methods of the present invention avoid the problem of solving for the light sources that produced  
10 the query image by using each successive 3D model as a candidate solution, and in conjunction with the query, building a histogram-like table that specifies a brightness coefficient for each surface normal which depends only on the normal. In one variation of the methods of the present invention, the model is then rendered in the already approximately known pose using these brightness coefficients, and the resulting image is compared to the query image and an error is computed. This error determines a ranking of the models for the purpose of identification. In another variation, no rendering is done, and instead the variance of the samples in each "bucket" of the brightness vs. normal  
20 histogram-like table is computed, and this variance, possibly weighted by the number of samples is summed over all buckets to yield a quality measure, which is then used for identification in the same way as an error measure.

25 It is assumed that there is a good, though not necessarily exact, solution for the pose of the query. However, it is not known which model generated the query image, and it is not known what were the lighting conditions for the query.

30 The method of the present invention therefore proceeds as follows:

a. Assume, in turn, that each model is the "correct" one.

b. Using the query image, compute a histogram-like table that associates a "brightness" coefficient with each normal. (For color images, three such coefficients are preferably computed, one for each color component, typically red, green, and blue).

5

There are then 2 preferable variations for the method. The first is as follows:

10

c1. Use the normals of the model under consideration in conjunction with the normal/brightness histogram computed in step (b) to render a picture of the model under putatively the same lighting conditions as were present when the query was photographed.

d1. Compare the query with the rendered picture to rank the likelihood that this model is in fact the correct one.

The second variation replaces the last 2 steps with these:

20

c2. Having saved additional information when constructing the normal/brightness histogram, compute the variance of the brightness coefficients that were used to compute each bucket of the histogram. (A "bucket" is the set of similar normal values that are lumped together to form a single argument value in the histogram.)

25

30

d2. Compute the sum of the variances of the histogram buckets, weighted by the number of samples in each bucket. Use this sum as an error measure in ranking the models to select the correct one.

In step (b), solving for the lighting in the paradigm that was discussed above as step (2) is avoided. However, in step (c1), it is still possible to perform the rendering that is called for

in step (3) of the paradigm. In the alternate evaluation steps, (c2) and (c3), it is possible to avoid rendering altogether in assessing the likelihood of a match between a 3D model and a 2D photograph query.

5

The methods of the present invention are thus based on the observation that computing the light sources, i.e. the lighting, that produced the query image, is only an intermediate step in a process whose real goal, in the context of the overall system, is to render the identification candidate under those lighting conditions for the purposes of comparison to the query, or indeed to compute the relative likelihood that the model matches the query even without doing such a rendering but with equivalent results.

10

What is ultimately being measured is the consistency of the imputed brightness coefficients associated with each normal. Because the 3D model's normals and reflectance values are used in conjunction with the query's observed intensities, this is a measure of the error in fitting the 2D photograph query to the 3D model.

20

The methods of the present invention are based on a Lambertian model of reflectance. The Lambertian assumption is that the intensity projected onto a point in a monochrome photograph of an object lit by a point source of light depends only on the following quantities:

25

R, the "reflectance" at the point of the object that gives rise to the corresponding point in the picture,

30

N, the "normal" to the surface at the point in question (i.e. the unique perpendicular direction to the surface at that point),



L, a unit vector representing the direction from the point to the light, and

b, the intensity of the light source at the point.

5

In particular, the observed intensity in the picture does not depend on the viewpoint, but only on the intrinsic properties of the object, and the lighting direction and intensity.

10 The observed image intensity is described by the equation:

$$I = R \cdot b \cdot L \cdot N \quad (3)$$

where I is the image intensity at the image point in question, and  $\cdot$  is the usual vector dot product.

If the quantities R, b, L, and N are given at each point, then in order to make a rendering from a 3D model, one need only perform the multiplications in equation 3. Also, it must be determined which portions of the model will be visible; however, that can be performed adequately by existing computer graphics techniques.

The situation in the model identification problem being solved is that R and N are known for each model, I is known from the query, and b and L are unknown. One approach, involving step (2) in the paradigm discussed above, is to solve for b and L, and then perform the multiplication in equation 3.

The approach of the methods of the present invention is to attempt to solve only for the composite quantity  $b \cdot L \cdot N$ , and then (in the first variation mentioned above) perform the multiplication in equation 3.

At each point, equation 3 is divided to give

$$b L * N = I/R \quad (4)$$

call this quantity  $B(N)$ , a brightness coefficient.

5 After rendering, equation 3 becomes

$$I_{\text{rendered}} = B(N) R \quad (5)$$

10 If this were done at just one point, this is a triviality, and we would simply get back the query's 'I' that we started with. However, in general, for every normal that occurs in the model, there will be many other points with the same or nearly the same normal. If all the B values that we get are averaged whenever the same normal occurs, and equation 5 is used to render a picture from the model, we will get only an approximation to the 'I' in the query. If the different values that were averaged to obtain  $B(N)$  for a given N were different due to small variations in material properties, measurement error, nonlinearities, etc., but the query did in truth match the model, then it can be expected that the average represented by  $B(N)$  would be a good approximation to the number needed for equation 5 to give a good approximation to the observed query intensity. However, when the query does not in truth match the model, because the values of N that are being used come from the model, while the intensities, I, come from the query, it can be expected that the correlation among  $B(N)$  values will be poor, and the average, when inserted into equation 5 for rendering, is unlikely to give a result which is close to the value in the query. In that case the rendering will be found to have a larger error from the query than in the case where the query in truth did match the model.

15  
20  
25  
30

B is a function which takes a surface normal vector to a number, i.e.,  $B: S^2 \rightarrow R$  where  $S^2$  is the so-called Gaussian sphere, which is the space (or manifold) of all possible normal

directions to a surface embedded in 3 dimensional space. The 2  
denotes the fact that this sphere is 2-dimensional, like the  
surface of a common ball. For this reason, the method of the  
present invention is referred to as the "lightsphere" method,  
5 since it attempts to find a brightness function defined on the  
Gaussian sphere.

So far, the situation has been presented with a single point  
light source and a monochrome picture. To generalize from  
10 monochrome to color, the monochrome case is done 3 times, once  
for each color component.

Generalizing the lighting, other than its color, is not as  
simple. In general the lighting can be, and usually is, much  
more complex than a simple point source. Any point of the  
surface can have light impinging on it from all directions, in  
the hemisphere visible to it, and this lighting can vary from  
point to point. At each point, the lighting is also a function  
on the Gaussian sphere, prescribing the intensity of light coming  
from the direction represented by that point on the Gaussian  
sphere. In general, this function can vary from point to point  
throughout space, and therefore can vary on the surface we are  
imaging. If the further assumption is made that all the lights  
are infinitely far away, then the lighting function does not  
25 vary from point to point, and the global lighting can be thought  
of as a function on the Gaussian sphere.

To generalize equation 3 to this situation, we simply integrate  
over the Gaussian sphere, or approximate the integration by a  
30 summation. There is a small complication in that a nonlinearity  
is introduced because only the lights with a direction that  
result in a positive dot product with N make a contribution;  
there is no negative brightness from lights behind the surface.  
However, this does not disturb the key point, which is that the

new lighting equation, which is now something of the form

$$I = R f(N) \quad (6)$$

5 still uses the exact same light distribution whenever the same  
normal is encountered, and therefore the computation of equation  
4 and the rendering of equation 5 are just as valid as with a  
single point source. It should be noted that for both equation 3  
and equation 6 to be independent of position and depend only on  
10 normal, it is assumed that there are no "cast shadows". Cast  
shadows are shadows that are caused by non-local interactions,  
such as when the nose casts a shadow onto the cheek; these are  
distinguished from "attached shadows" which occur as the object  
smoothly curves away from the light source, as occurs when only  
the lit part of the moon is visible at night. The methods of the  
present invention neglect the effect of cast shadows.

15 In fact, with more complex lighting, when we are attempting to  
match a wrong model, the fact that different light sources will  
come into play in the query, for the same normals on the model,  
will result in an even larger error when matching the wrong  
20 model, with no similar increase in error when matching the  
correct model. Hence, this lighting nonlinearity actually  
enhances the effectiveness of the invention.

25 A similar observation applies with regard to specularities. The  
location of specularities in an image violates the Lambertian  
assumption of equation 3 in two important ways:

- 30 1. The location of the specularity depends on the camera  
viewpoint; and
2. The brightness of the specularity does not vary linearly with  
either the lighting vector or the normal vector.

These problems make it difficult to incorporate specularity into any system which must solve for light sources, though it is by no means impossible. Consequently, specularities often lead to increased error.

However, if we continue to assume that the light sources are at infinity, and there are no cast shadows, then even in the presence of specular reflection, equation 6 still applies approximately. More specifically, the new equation is

$$I = R f(N) + S g(N) \quad (7)$$

where  $S g(N)$  represents the specular component of the reflected light.  $S$  is the shininess of a particular point of the surface, in analogy to  $R$ , while  $g(N)$  captures the intensity variation as a function of the normal.

When we apply the lightsphere calculation of equation 4 to equation 7 we get

$$I/R = f(N) + S g(N)/R \quad (8)$$

However, if this is to be  $B(N)$ , a problem arises because  $R$  and  $S$  depend on the position on the surface, and not on the normal. This means that the quality of the rendering that can be achieved with the  $B(N)$  that can be computed as the average of the above values  $I/R$  will depend on the degree of variation of  $R$  and  $S$  at the normals involved. Nevertheless, the rendering will approximate some specular component where it exists, and will therefore be closer to the exactly correct rendering than one based simply on rendering from computed lights with a Lambertian rendering equation. Of course, with another method, one can compute the lights based on some nonlinear model that includes specularity, and render with that model. However, in the methods

of the present invention, this is achieved at no increase in complexity; with other methods, the specular reflectance equation would have to be explicitly modeled, with a concomitant increase in complexity and computational cost.

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Conversely, when the wrong model is rendered for the query, because specularities tend to have quite bright components, wildly inappropriate values for  $B(N)$  are expected when there are specularities. This leads to proportionately greater error added to the wrong model's ranking than to the right one's. Hence, specularity in the query can actually enhance the effectiveness of the invention.

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We note that the measures corresponding to the two variations of the methods of the present invention are closely related. The two measures are, respectively, (1) error between rendered image and query, and (2) weighted variance of lightsphere coefficient values within each bin. Each coefficient that entered into the variance computation arose from a point in the query. When that point is rendered with the average lightsphere coefficient for its normal's bin, the error will be proportional (via the reflectance) to the difference between the average coefficient being used in the rendering and the exact coefficient that was used in computing the average. Were it not for the reflectance multiplier, when summing over the points that fall into the bin, the sum of the squares of the one set of errors is the same as the sum of squares of the differences, and the latter is exactly the variance of the bin weighted by the number of samples. Thus, the two measures differ only by a weighting factor of reflectance in the error sums. It is to be noted that by error between images, it is meant RMS (root mean square) error, or equivalently, SSD (sum of squared differences). Other error measures are possible, as well.

The invention is intended as a component in a larger system whose function is to store numerous 3D models of objects, and upon presentation of a query image to provide the most likely stored model corresponding to the query. A schematic illustration of such a system is presented in Fig. 1. Asynchronously, and over arbitrary lengths of time, the system is presented with 3D objects 10, typically human heads and preferably human faces, which it scans and digitizes with a scanning device 20, at the same time capturing the reflected light image at all included 3D data points. A reflectance estimation module 30 computes a reflectance function for the 3D object 10. This information is then stored in a database 40. This storage can include information about surface normals, or surface normals can be computed as needed at later stages when the data is to be used.

At an arbitrary time, a query photograph 50 is presented to the system for identification. A lightsphere 60 is used to compare the 2D query 50 to each of the stored 3D models 10 and to select a best match 70. Not shown is a separate module which computes the pose for a given query and model, possibly based on other stored data. This pose information is needed by the lightsphere module 60.

Fig. 2 illustrates the lightsphere module 60 of Fig. 1 in greater detail. The query image 50 is presented for identification. The lightsphere module 60 has a sub module 140 which sequentially considers one model 10 at a time for similarity to the query image 50. To do this it obtains the next model 50 from the database 40, and obtains from a pose module 120 the pose solution for that model 10 and query image 50. This is needed to establish the putative corresponding points of the query image 50 and the model 10. The pose solution operation may have been done earlier for all models 10 with this query image 50, or it may be done upon demand by the lightsphere module 60.





under the Lambertian model we expect to be the same as  
b L \* N (2). The value of N (220) that is known for this point  
from the model 10 is the value used to choose the correct bin 200  
of the data structure 160, and the value I/R is then inserted  
5 (230) into this bin 200, either by summing, or recording the  
values inserted into the bin 200, depending on which variation of  
the methods of the present invention is being used.

Although the model evaluation process has been presented as a  
10 sequential one, where only one model is being evaluated at any  
time, as discussed above, it is possible to divide attention  
among numerous models using partial solutions so that the cost of  
fully evaluating a model is only expended if the model continues  
to have a low error in competition with other models.

Also, prior to the final error ranking process, lightsphere  
results for one model do not require results for any other model.  
Consequently, the overall process trivially admits of massive  
parallelization, with a proportional increase in overall speed.

The lightsphere module 60 will now be described in greater  
detail. The lightsphere module 60 can be divided into two  
stages:

25 1. Preprocessing steps that:

a. Compute the pose of the model that best accounts for the  
query.

30 b. Generate a registered map of the surface normals of the  
model corresponding to points on the query.

c. Generate a registered image of the model's reflectance  
corresponding to points on the query.



$$Q: R^2 \rightarrow R^+ \quad (9)$$

This notation means that  $Q$  is a map from the 2-dimensional real Euclidean plane to the nonnegative real numbers. It is assumed that  $Q$  only takes nonzero values, or is only defined, in some finite rectangle of the plane. In actual fact,  $Q$  is sampled at only a finite discrete grid of points, so that it takes values at only integer coordinate values. Note that  $Q$  is a function, while the notation  $Q(p)$ , where  $p$  is a point in  $R^2$ , denotes the real number to which  $Q$  maps the point  $p$ .

The 3D model  $M$  consists of several subparts. These include a set of  $n$  points

$$\{p_i \mid i = (1, 2, \dots, n)\} \quad (10)$$

in  $R^3$  which are the locations of sample points on the model, and a corresponding set of  $n$  real numbers  $r_i$  which represent the surface reflectance at each corresponding  $p_i$ .

The camera model  $K$  is a perspective projection. I.e.,

$$K: R^3 \rightarrow R^2 \quad (11)$$

where, after some change of coordinate systems by rigid motion,

$$K(x, y, z) = a^*(x, y)/z, \quad (12)$$

for some positive real number  $a$ . The change of coordinates is part of the camera model. There are many other ways to formulate the definition of perspective projection; this one is equivalent, and the exact formulation is not important. For the purposes of the lightsphere computation, distortion effects of the camera are

not considered, and the camera model is fixed. Variations where more information about the camera is used are obvious. Note that this definition allows for some amount of perspective distortion, depending on the values of the camera model  $K$  and the position of the 3D model in space. However, to the degree that the true camera and subject location for the query lead to more or less perspective distortion, this difference is not compensated for in what is described below, although a more detailed camera model could accomplish this.

The pose  $T$  is the rigid motion in  $R^3$  which, when applied to the model  $M$ , after projection through the camera model  $K$ , brings the image of the model  $M$  into the best registration with the query  $Q$ .

I.e., the pose  $T$  tries to satisfy the following equation:

$$K(T(p_i)) = q_i \quad (13)$$

where  $p_i$  is a point of the 3D model, and  $q_i$  is the corresponding point of the query image, simultaneously for some set of points  $p_i$  and  $q_i$ .

The registered reflectance image  $R$  is a map

$$R: R^2 \rightarrow R^+ \quad (14)$$

(Note that the first  $R$  is a different  $R$  than the 2nd and 3<sup>rd</sup>.) sampled on the same grid as the query image  $Q$ , such that

$$R(K(T(p_i))) = r_i \quad (15)$$

In other words,  $R$  tells us, given a point in the query image  $Q$ , what the reflectance is of the point in the model that projects to that point in the query given the pose and camera model. Note

that several points on the model might project to a single point in the query; i.e. the computer graphics technique of hidden surface elimination is necessary to find the unique R that corresponds to the surfaces of the model that are actually visible under the assumed pose and camera model. Numerous well-known computer graphics techniques exist that can accomplish this. Both proprietary and freely available packages have been used to do this computation with equal success.

The surface normal  $n_i$  to a point  $p_i$  of the 3D model M is a unit vector in  $R^3$  which represents the direction at right angles to the surface of M at  $p_i$ . Computing  $n_i$  requires knowing some nearby points of M, i.e. nearby on the surface that M represents. In our apparatus, this is known in advance because the data in M comes from a system that essentially produces a raster scan. In addition, there are standard computer graphics techniques that allow putting a less ordered set of points into a form where such neighboring points are known, for example, by the process known as triangularization of the surface. If p has the neighbors q and s, then the unit normal at p can be computed by

$$v = (p-q) \times (p-s) \quad (16)$$

$$n = v / ||v|| \quad (17)$$

where  $\times$  is the vector cross-product, and  $||v||$  is the norm of v.

In practice, it is often better to consider several neighbors of p, e.g. in a grid, the 8 or 4 neighbors, and take the average of the values thus computed.

Because n is a vector in  $R^3$  it can be written as

$$n = (n_x, n_y, n_z) \quad (18)$$

where the three components are the components of  $n$  in the  $x$ ,  $y$ , and  $z$  directions, respectively. However, the requirement that  $n$  be a unit vector imposes the constraint that

$$1 = ||n||^2 = n_x^2 + n_y^2 + n_z^2 \quad (19)$$

This can be viewed as the equation of a 2-sphere, i.e., the surface of a ball in 3-space. Geometrically, if  $n$  is considered to be anchored at the origin, as  $n$  varies among all possible values for a unit vector, its tip varies over the surface of the unit sphere. Therefore each  $n$  can be identified with these tip positions, i.e. with the points of the 2-sphere. The 2-sphere is commonly denoted by  $S^2$ .

When this identification is made between the unit normals of a surface and the 2-sphere in differential geometry, the sphere is commonly referred to as the "Gaussian sphere", and the map which maps each point of the surface to its normal is known as the "Gauss map".

With this in mind, the registered normal map can be defined as a map

$$N: R^2 \rightarrow S^2 \quad (20)$$

which takes each point in the query image  $Q$ , to the surface normal at the point of the 3D model  $M$  which projects to that point of  $Q$  under the pose  $T$  and camera model  $K$ . I.e.,  $N$  is defined to satisfy

$$N(K(T(p_i))) = n_i \quad (21)$$

in analogy to the similar equation (15) for the registered reflectance, where now  $n_i$  is the normal calculated in the

preprocessing stage at the point  $p_i$  .

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N, again, is calculated only at the grid points associated with the grid points of Q. The calculation of N, like the calculation of R, requires hidden surface removal to guarantee that only the value of n for the visible surface is used. Again, this is most easily done by using existing standard computer graphics techniques. One can take advantage of existing graphics interfaces to do this by allowing the graphics engine to compute renderings with 6 different light sources: one for each combination of positive and negative coordinate direction, i.e., lights coming from +-x, +-y, +-z. With a Lambertian rendering model in the graphics engine, these will yield the positive and negative components of the normal vector at each point. This also allows the use of the graphics engine's techniques for interpolation, which helps considerably in the performance of the algorithm.

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The lightsphere algorithm calculates a normal-lightness table B from the query Q, the registered reflectance image R, and the registered normal map N.

Before we define and describe how to compute B, consider first the map

$$A: S^2 \rightarrow R^+ \quad (21)$$

given by

$$A(n) = Q(q)/R(q) \quad (22)$$

when  $N(q) = n$ .

For notational compactness, define

$$D: R^2 \rightarrow R^+ \quad (23)$$

$$\text{by } D(q) = Q(q)/R(q). \quad (24)$$

5 (Elsewhere this is referred to as I/R.)

We would like A to be defined by  $A(n) = D(N^{-1}(n))$ . However, there may be many points where the normal is n, so that  $N^{-1}(n)$  is not a single point, but a set of points. To estimate A, it is  
10 desirable to take the average of D on this set of points. I.e., suppose that

$$P(n) = \{p \mid N(p) = n\} \quad (25)$$

is the set of points in the query that map to the normal n. Our goal is to define A by

$$A(n) = \frac{1}{\#(P(n))} \sum_{p \in P(n)} D(p) \quad (26)$$

where  $\#(P(n))$  is the number of points in the set  $P(n)$  (or the measure of the set, in the continuous case). This is a well-defined quantity.

However, this is not adequate when a discrete grid, in this case the discrete grid of the query image is being operated on. The problem is that the normals are derived from the 3D model, and in  
30 general the values to which they have been discretized depend only on the accuracy of the 3D model data and the method whereby the normals were computed. In particular, they will generally be discretized to such a fine degree that it is unlikely that any two of the discretized points  $q_i$  of the query will map to the  
35 same normal n, and therefore almost every  $A(n)$  will arise from only a single sample. In that case, the lightsphere calculation,



when used to render an image from the model will be trivial, i.e., it will result in exactly the query image value, since we will simply be computing the quantity

$$I(p) = A(N(p)) \quad R(p) = D(p) \quad R(p) = Q(p)/R(p) \quad R(p) = Q(p) \quad (27)$$

Therefore, it is essential that a way be devised that in general, several values will be averaged to obtain  $A(n)$ . A way to do this is to discretize the Gaussian sphere into a small enough number of bins (or buckets) that a sufficient number of buckets contain more than one sample. There are numerous ways to discretize the 2-sphere. For example, one can take an icosahedron centered at the same point as the sphere and radially project the icosahedron to the sphere. This gives a partition, or tessellation, of the sphere. However, for our purposes it has been found that it works well to use an extremely simple method of discretizing the sphere, which can now be described.

We start with a unit normal vector

$$n = (n_x, n_y, n_z) \quad (28)$$

In the methods of the present invention, surface normals that point away from the camera are not of interest, because the camera cannot see any surface point that has such a normal. By "point away from the camera", it is meant that if  $v$  is a vector that points in the direction of the camera perspective projection center from the point  $p$  on the surface, and  $n$  is the outward pointing normal at the point  $p$ , then if  $n \cdot v < 0$ , where  $\cdot$  is the vector dot product, we say that  $n$  is pointing away from the camera. Thus only normals  $n$  on half of the Gaussian sphere are of interest, the half where the above inequality does not hold. Let us for the moment use a coordinate system where the camera axis lies along the  $z$  axis and the camera is in the positive  $z$

direction from the subject. Then the set of all surface normals we are interested in is exactly those where  $n_z > 0$ . This can be thought of as a hemispheric cap lying on the x-y plane.

Now our goal is to discretize this hemispheric cap based on the values  $n_x$ ,  $n_y$ ,  $n_z$ . The easiest way to do this is to ignore the z component altogether, and consider only the projection of the hemispheric cap onto the x-y plane, which is a circular disk. We will discretize this disk, and define the discretization of the hemisphere by the projection back up along z from the plane to the hemisphere. To discretize this disk, the unit disk in the plane, we will simply discretize the unit square in the plane, and restrict it to the disk. To simplify the next discussion, consider the unit square to be the part of the plane given by

$$0 \leq x < 1 \quad \text{and} \quad 0 \leq y < 1. \quad (29)$$

(Since the values of the unit normal components vary from -1 to +1, this involves a scale and shift; in an actual program, one would probably not bother to do this).

The way to do this is as follows. We will discretize so that there are m bins, i.e., into an m x m square tessellation. Divide the unit square into  $m^2$  subsquares  $S_{ij}$ ,  $i, j = 1, 2, \dots, m$ , as follows. A point p of the unit square is in subsquare  $S_{ij}$  if

$$(i-1)/m \leq p_x < i/m \quad \text{and} \quad (30)$$

$$(j-1)/m \leq p_y < j/m \quad (31)$$

where  $p_x$  is the x coordinate of p and  $p_y$  the y coordinate.

Then considering each subsquare  $S_{ij}$  a "bin" or "bucket", we say that p falls into the (i,j)th bucket if the above conditions (30)

and (31) are satisfied.

Using this definition, a unique bucket  $(i,j)$  can be defined for each unit normal  $n$  as follows. First, because a shift and scale was done, define

$$n' = [n + (1,1,0)]/2 \quad (32)$$

This moves and shrinks the hemisphere to lie over the unit square as it was defined above. (This is only necessary because simple notation is desirable; this entire analysis is identical with a square that goes from -1 to +1 in  $x$  and  $y$ .)

Now just compute  $i$  and  $j$  according to (30) and (31), using  $n'_x$  in place of  $p_x$  and  $n'_y$  in place of  $p_y$ ,  $n_z$  is simply ignored, which has the effect of projecting the square up to the hemisphere. These  $(i,j)$  coordinates define the bins for the basic lightsphere procedure. Note that these are not of uniform size on the Gaussian sphere; however, this is not very significant in practice, as they are uniform in the query image.

Now the algorithm can proceed by systematically iterating through the points of the query image. First, it must keep 2 items of data for each bin: a running sum, and a count of the number of samples used thus far in the sum. (Since the count is used to compute an average, an updating method could be used to maintain only a single number for each bin, but this is not worth the bother since the table is small.) Then as the algorithm iterates through the query image  $Q$ , at each point  $p$  it refers to the reflectance image  $R$  and the normal map  $N$ . It computes the value of  $D(p) = Q(p)/R(p)$  and adds this value to the  $(i,j)$ th bin where  $(i,j)$  are computed according to (30) and (31) from the value of the normal  $N(p)$ . (With the understanding that by this it is meant that the same scale and shift operation that gave  $n'$  above

is taken into account, here and in what follows.) Also it increments the count for the (i,j)th bin. Once it has finished iterating through the query image, it divides the sum at each bin by the count at that bin to arrive at an average. This results in a table of numbers B(i,j) that are the B(n) mentioned above, the lightness table.

In practice, as explained above, additional criteria are used to decide whether to include a particular query image point in the above computation. For example, image points that are too bright or too dark are excluded.

So far the methods of the present invention have been explained for the variation where the error between a rendered image of the model and the query image as our quality criterion is used.

To render an image using the lightsphere data structure B(i,j) the algorithm proceeds as follows. It iterates through the registered reflectance image R. At each point p of R, it looks up the normal N(p) in the registered normal map N. Using the value of N(p) thus retrieved, it computes the corresponding lightsphere bin (i,j) using (30) and (31), and retrieves the value B(i,j). It then computes

$$I(p) = R(p) B(i,j) \quad (33)$$

and sets the brightness value of the rendered image I to that value, after clipping to avoid values larger than the maximum brightness.

Actually, there is an additional step before the last computation is done. Because there are a very small number of bins compared to the number of actual normal values, using the value B(i,j) directly as above results in considerable artifact due to the

coarse digitization of the bins. Therefore, instead an interpolated value  $B'(p)$  is used. The interpolation is based on the value of the normal  $N(p)$ . Since we know where  $N(p)$  falls in the square defined by the  $(i,j)$ th bin, we simply use bilinear interpolation with the adjacent values of  $B(i,j)$  to arrive at the interpolated  $B'(p)$ , which is then used to compute

$$I(p) = R(p) B'(p) . \quad (34)$$

The error  $E$  is then computed as the sum of square differences or root mean square error between the query image  $Q$  and the rendered synthetic image  $I$ , which are already registered by virtue of the method of construction of  $I$ .

Now we return to the variations of the algorithm that use the variances of the lightsphere. This proceeds identically to what was described above, except that the data that is associated with each bin is slightly more complex. Rather than keep a running sum and a count for each bin, instead for each bin a list is kept of all the  $D(p)$  values that fell into that bin. When the iteration is completed, the mean and variance of the list of values in each bin is computed for that bin. The mean is identical to  $B(i,j)$  defined above. In addition, we also now have the variances  $V(i,j)$ .

In the first variation using variances, the error  $E$  is defined as the sum of these variances, i.e.,

$$E = \sum_{i,j} V(i,j) \quad (35)$$

In the second such variation, we want to weight this sum by the counts, which will be more similar to the sum of square differences between the rendered and query images used earlier.

Call the counts that were kept in the accumulation process  
C(i,j). Then in this variation, the error measure is given by

$$E = \sum_{i,j} C(i,j) V(i,j) \quad (36)$$

It should be noted that although a few very specific methods to  
accomplish the lightsphere computation have been presented, there  
are other formulas and algorithms that could be used for the  
various components and for the error term. These equations and  
explanations are merely the description of one possible way to  
achieve an embodiment of the invention, and many other ways are  
possible with simple modifications and/or additions.

#### EXAMPLE

The methods of the present invention have been actually reduced  
to practice in both the C and C++ programming languages and  
tested on a pilot database containing 37 3D models, and actual  
queries consisting of 37 subjects in all combinations of 7 poses  
and 6 lighting conditions.

Several additional techniques can be utilized to optimize the  
performance of the methods of the present invention which have  
been actually reduced to practice.

1. It has been found that a grid of 32x32 bins for the  
lightsphere histogram works well for images and models with a  
resolution of 640x640. 24x24 bins also works well. The number  
of bins imposes a tradeoff between accuracy in the brightness  
coefficient -- the accuracy increases as there are more bins,  
since a smaller range of normals is used in the averaging -- and  
statistical significance of the average, which improves as the  
number of bins is decreased, since a greater number of normals

then fall into each bin. Thus, the methods of the present invention can be further improved by estimating the magnitude of these effects upon seeing the data and choosing an appropriate number of bins.

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2. It is possible to use a tessellation of the Gaussian sphere for the bins. This improves the performance at the expense of a slightly greater cost in computing the lightsphere histogram and rendering from it. Furthermore, it has been found that  
10 projecting a tessellation of the unit disk onto the Gaussian sphere, i.e. using only x and y values, not z, for determining the bins, is quite effective, despite the sampling inequities it introduces.

3. Because the histogram bins are quite coarse relative to the image and model resolutions, it has been found that bilinear interpolation of the lightsphere values when doing rendering greatly improves both appearance and accuracy.

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4. For a Lambertian object, the dot product in the integral which gives the image intensity reduces to a cosine between normal and light directions. The resulting image intensity as a function of normal is essentially a convolution of this cosine with the light intensity distribution. This amounts to a low pass filter operation in the absence of cast shadow. Thus, in a system which solves for lighting and then does rendering, there would be enforced a smoothness upon the brightnesses as a function of normal by virtue of this convolution. In the methods of the present invention, the lightsphere computation does not  
contain such a mechanism to enforce smoothness. Consequently, the lightsphere data can contain variations with high frequency components that result from multiple sources, such as departure from Lambertian, reflectance errors, etc. Therefore, it has been found useful to do a small amount of smoothing on the lightsphere

histogram. This can be done by a convolution with a simple small box function. This significantly improves the rendering and the performance of the method.

5 5. When using equation 4 to compute the lightsphere data structure, points with very low reflectance can contribute enormous numbers when the division is performed. Such points lead to meaningless results. To avoid this problem, a minimum threshold is used which the reflectance must exceed before it can enter into the computation. This threshold is currently set ad hoc; however, it could also be computed based on inspecting the reflectance histogram, and stored once and for all with each model. Since the computation of this threshold can be performed at the time the model is added to the database, arbitrarily sophisticated methods could be used to compute it. As an extreme example, it could be set to provide optimum differentiation from other models in the database, based on synthetic renderings of numerous models.

20 6. Extreme specularities tend to be associated with points, such as areas in the eye, where the range data is unreliable. In addition, such points tend to saturate the intensity scale. Therefore it is preferable to impose a maximum threshold which intensity values must not exceed in order to be included in the lightsphere computation. Similarly, extremely dark areas of the query are strongly associated either with areas in cast shadow, or areas where reflectance computations mean little (such as hair). Both of these are sources of error for use, thus, a minimum threshold on intensity is also used in the query.

30 Those of skill in the art will appreciate that the methods of the present invention yield an identification of the object without the need for solving for light sources or other complex and costly computations such as eigenvector determination. Thus, the



methods of the present invention result in the following advantages over prior art methods:

1. A primary advantage over prior art methods is an enormous savings in computational cost. This savings can make the difference between practicality and impracticality in a complete system. For example, the methods of the prior art which use mutual information, while more general and perhaps more effective in principle, are prohibitively expensive for an application requiring a large number of comparisons with models.

2. The methods of the present invention are simpler than the prior art methods. The methods of the present invention required mainly the single process of building a histogram-like data structure, which is little more than visiting each point of the model, extracting the pre-stored normal and reflectance, and performing a few arithmetic steps to update the histogram (while the data structure is referred to as a histogram, it is really a slight generalization). By comparison, other methods require iterative algorithms that take one to two orders of magnitude more computer time on the size of problems involved. For example, one prior art method involves use of the so-called Nonnegative Least Squares algorithm, which is a complex iterative algorithm. Similarly, other approaches of the prior art require computing so-called Principal Components. These computations require finding an eigenvector decomposition, and again require complex iterative algorithms. While these more complex algorithms are well-known and understood, they are nevertheless vastly more complex than the methods of the present invention.

3. The methods of the present invention are more robust than other methods. Methods of the prior art typically depend on finding the solution to a system of linear equations under constraints, or in solving for linear invariants such as

eigenvectors. It is often hard to predict how the stability of these methods depends on the data and assumptions. Due to the straightforward nature of the methods of the present invention, unstable solutions are easily avoided.

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4. The methods of the present invention are amenable to use in a system where partial solutions can be used. For example, in considering a large number of candidate models for identification, many models can be discarded as soon as the error is known to be sufficiently large. Using the methods of the present invention, it is possible to interrupt computation of the error or quality term at numerous stages, and resume it only if needed at later stages. In the methods of the prior art, it is difficult or impossible to do this without incurring the full cost of the most expensive part of the method.

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5. The methods of the present invention are adaptable to unknown models of reflectance. Because light sources need not be computed, only the effect of lighting on the material being imaged is measured and assumed consistent. Even with specularities (shininess), the methods of the present invention allow for good results over a reasonable range of material properties.

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6. The methods of the present invention are robust against errors in capturing reflectance, particularly if lighting effects are present in the captured reflectance data.

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Since the methods of the present invention are extremely fast and do not require a great amount of computational effort, they may also be used in a system to winnow the candidate models that will be examined by more costly (and slower) methods by a factor of 10-100. These other methods are capable of a more precise identification, but are too costly for a very large database of

candidate models.

While there has been shown and described what is considered to be preferred embodiments of the invention, it will, of course, be understood that various modifications and changes in form or detail could readily be made without departing from the spirit of the invention. It is therefore intended that the invention be not limited to the exact forms described and illustrated, but should be constructed to cover all modifications that may fall within the scope of the appended claims.

WHAT IS CLAIMED IS:

1        1.        A method for matching a two dimensional image to one of  
2        a plurality of three dimensional candidate models, the method  
3        comprising the steps of:

4  
5                determining the position and orientation of the two  
6        dimensional image;

7  
8                for each three dimensional candidate model, computing a  
9        histogram-like table having a computed brightness coefficient for  
10       each surface normal of the three dimensional candidate model  
11       based on the corresponding value in the two dimensional image,  
12       each brightness coefficient depending only on the corresponding  
13       surface normal;

14  
15                successively rendering each three dimensional candidate  
16       model in the determined position and orientation using the  
17       surface normals in conjunction with the corresponding computed  
18       brightness histogram-like table; and

19  
20                comparing the two dimensional image with each of the  
21       rendered three dimensional candidate models.

22  
23       2.        The method of claim 1, further comprising the steps of  
24       determining if the two dimensional image matches one of the  
25       plurality of three dimensional models if the comparison between  
26       the two dimensional image and the rendered three dimensional  
27       model is within a predetermined allowable error.

28  
29       3.        The method of claim 1, wherein the comparison step  
30       results in a ranking for each of the rendered three dimensional  
31       models which indicates the likelihood that the corresponding  
32       three dimensional model matches the two dimensional image.

1 4. The method of claim 3, further comprising the step of  
2 choosing the three dimensional model corresponding to the  
3 rendered three dimensional model having the highest ranking as  
4 the three dimensional model which matches the two dimensional  
5 image.

1 5. The method of claim 1, further comprising the step of  
2 reading the three dimensional models from a database containing  
3 the plurality of three dimensional models.

1 6. The method of claim 1, wherein the comparing step is  
2 done simultaneously with the rendering step for each rendered  
3 three dimensional model.

1 7. The method of claim 1, wherein the computing step sets  
2 a minimum threshold of reflectance to be used in the computation  
3 of the histogram-like table.

1 8. The method of claim 1, wherein the computing step sets  
2 a minimum and/or maximum threshold of intensity to be used in the  
3 computation of the histogram-like table.

1 9. The method of claim 1, wherein the two dimensional  
2 image is a color image and wherein the a brightness coefficient  
3 is computed for each color component of the color image.

1 10. The method of claim 1, further comprising the step of  
2 smoothing the lightsphere histogram-like table to improve the  
3 rendering of each three dimensional model and the performance of  
4 the method.

1 11. The method of claim 10, wherein the smoothing step is  
2 done by a convolution with a small box function or other small

3 smoothing kernel.

1 12. A method for matching a two dimensional image to one of  
2 a plurality of three dimensional candidate models, the method  
3 comprising the steps of:

4  
5 determining the position and orientation of the two  
6 dimensional image;

7  
8 for each three dimensional candidate model, computing a  
9 histogram-like table having a computed brightness coefficient for  
10 each surface normal of the three dimensional candidate model  
11 based on the corresponding value in the two dimensional image,  
12 each brightness coefficient depending only on the corresponding  
13 surface normal;

14  
15 computing the variance of the brightness coefficients  
16 that are used to create each bucket of the histogram-like table,  
17 a bucket being a set of similar normal values that are lumped  
18 together to form a single argument value in the histogram-like  
19 table;

20  
21 computing the sum of the variances of the histogram-  
22 like table buckets; and

23  
24 ranking the three dimensional candidate models using  
25 its computed sum as an error function, the ranking indicating the  
26 likelihood that the corresponding three dimensional model matches  
27 the two dimensional image.

1 13. The method of claim 12, further comprising the step of  
2 choosing the three dimensional model corresponding to the three  
3 dimensional model having the highest ranking as the three  
4 dimensional model which matches the two dimensional image.

1 14. The method of claim 12, further comprising the step of  
2 reading the three dimensional models from a database containing  
3 the plurality of three dimensional models.

1 15. The method of claim 12, wherein the computing step sets  
2 a minimum threshold of reflectance to be used in the computation  
3 of the histogram-like table.

1 16. The method of claim 12, wherein the computing step sets  
2 a minimum and/or maximum threshold of intensity to be used in the  
3 computation of the histogram-like table.

1 17. The method of claim 12, wherein the two dimensional  
2 image is a color image and wherein the a brightness coefficient  
3 is computed for each color component of the color image.

1 18. The method of claim 12, wherein the sum of the  
2 variances are weighted by the number of samples in each bucket.

1 19. A method for matching a two dimensional image to one of  
2 a plurality of three dimensional candidate models, the method  
3 comprising the steps of:

4 determining the position and orientation of an object  
5 giving rise to the two dimensional image;

6  
7  
8 computing a representation of lighting effects that  
9 allows the lighting that gave rise to the two dimensional image  
10 to be used to render a realistic image of a three dimensional  
11 candidate model;

12  
13 successively rendering each three dimensional candidate  
14 model in the determined position and orientation using the

15 surface normals in conjunction with the corresponding computed  
16 representation of lighting effects; and

17  
18 comparing the two dimensional image with each of the  
19 rendered three dimensional candidate models.

1 20. A method for matching a two dimensional image to one of  
2 a plurality of three dimensional candidate models, the method  
3 comprising the steps of:

4  
5 determining the position and orientation of an object  
6 giving rise to the two dimensional image;

7  
8 computing a representation of lighting effects based on  
9 the plurality of three dimensional candidate models and the two  
10 dimensional image that allows evaluation of the likelihood that a  
11 particular three dimensional candidate model gave rise to a  
particular two dimensional image; and

12  
13 choosing the most likely three dimensional candidate  
14 model to have generated the query based on the computed  
15 representation of lighting effects.  
16

17  
18 21. A computer program product embodied in a computer-  
19 readable medium for matching a two dimensional image to one of a  
20 plurality of three dimensional candidate models stored in a  
21 database, the computer program product comprising:

2  
3 computer readable program code means for determining  
4 the position and orientation of the two dimensional image;

5  
6 computer readable program code means for computing a  
7 histogram-like table each three dimensional candidate model,  
8 having a computed brightness coefficient for each surface normal  
9  
10  
11



12 of the three dimensional candidate model based on the  
13 corresponding value in the two dimensional image, each brightness  
14 coefficient depending only on the corresponding surface normal;

15  
16 computer readable program code means for successively  
17 rendering each three dimensional candidate model in the  
18 determined position and orientation using the surface normals in  
19 conjunction with the corresponding computed brightness histogram-  
20 like table; and

21  
22 computer readable program code means for comparing the  
23 two dimensional image with each of the rendered three dimensional  
24 candidate models.

25 22. A program storage device readable by machine, tangibly  
26 embodying a program of instructions executable by the machine to  
27 perform method steps for matching a two dimensional image to one  
28 of a plurality of three dimensional candidate models, the method  
29 comprising the steps of:

30 determining the position and orientation of the two  
31 dimensional image;

32 for each three dimensional candidate model, computing a  
33 histogram-like table having a computed brightness coefficient for  
34 each surface normal of the three dimensional candidate model  
35 based on the corresponding value in the two dimensional image,  
36 each brightness coefficient depending only on the corresponding  
37 surface normal;

38 successively rendering each three dimensional candidate  
39 model in the determined position and orientation using the  
40 surface normals in conjunction with the corresponding computed  
41 brightness histogram-like table; and

21 comparing the two dimensional image with each of the  
22 rendered three dimensional candidate models.

1 23. A computer program product embodied in a computer-  
2 readable medium for matching a two dimensional image to one of a  
3 plurality of three dimensional candidate models stored in a  
4 database, the computer program product comprising:

5  
6 computer readable program code means for determining  
7 the position and orientation of the two dimensional image;

8  
9 computer readable program code means for computing a  
10 histogram-like table for each three dimensional candidate model,  
11 having a computed brightness coefficient for each surface normal  
12 of the three dimensional candidate model based on the  
13 corresponding value in the two dimensional image, each brightness  
14 coefficient depending only on the corresponding surface normal;

15  
16 computer readable program code means for computing the  
17 variance of the brightness coefficients that are used to create  
18 each bucket of the histogram-like table, a bucket being a set of  
19 similar normal values that are lumped together to form a single  
20 argument value in the histogram-like table;

21  
22 computer readable program code means for computing the  
23 sum of the variances of the histogram-like table buckets; and

24  
25 computer readable program code means for ranking the  
26 three dimensional candidate models using its computed sum as an  
27 error function, the ranking indicating the likelihood that the  
28 corresponding three dimensional model matches the two dimensional  
29 image.

1 24. A program storage device readable by machine, tangibly

2 embodying a program of instructions executable by the machine to  
3 perform method steps for matching a two dimensional image to one  
4 of a plurality of three dimensional candidate models, the method  
5 comprising the steps of:

6  
7           determining the position and orientation of the two  
8 dimensional image;

9  
10           for each three dimensional candidate model, computing a  
11 histogram-like table having a computed brightness coefficient for  
12 each surface normal of the three dimensional candidate model  
13 based on the corresponding value in the two dimensional image,  
14 each brightness coefficient depending only on the corresponding  
15 surface normal;

16  
17           computing the variance of the brightness coefficients  
18 that are used to create each bucket of the histogram-like table,  
19 a bucket being a set of similar normal values that are lumped  
20 together to form a single argument value in the histogram-like  
21 table;

22  
23           computing the sum of the variances of the histogram-  
24 like table buckets; and

25  
26           ranking the three dimensional models using its computed  
27 sum as an error function, the ranking indicating the likelihood  
28 that the corresponding three dimensional candidate model matches  
29 the two dimensional image.

1   25.       A computer program product embodied in a computer-  
2 readable medium for matching a two dimensional image to one of a  
3 plurality of three dimensional candidate models stored in a  
4 database, the computer program product comprising:

6 computer readable program code means for determining  
7 the position and orientation of an object giving rise to the two  
8 dimensional image;

10 computer readable program code means for computing a  
11 representation of lighting effects that allows the lighting that  
12 gave rise to the two dimensional image to be used to render a  
13 realistic image of a three dimensional candidate model;

15 computer readable program code means for successively  
16 rendering each three dimensional candidate model in the  
17 determined position and orientation using the surface normals in  
18 conjunction with the corresponding computed representation of  
19 lighting effects; and

21 computer readable program code means for comparing the  
22 two dimensional image with each of the rendered three dimensional  
23 candidate models.

26. A program storage device readable by machine, tangibly  
embodying a program of instructions executable by the machine to  
perform method steps for matching a two dimensional image to one  
of a plurality of three dimensional candidate models, the method  
comprising the steps of:

7 determining the position and orientation of an object  
8 giving rise to the two dimensional image;

10 computing a representation of lighting effects that  
11 allows the lighting that gave rise to the two dimensional image  
12 to be used to render a realistic image of a three dimensional  
13 candidate model;

15 successively rendering each three dimensional candidate

16 model in the determined position and orientation using the  
17 surface normals in conjunction with the corresponding computed  
18 representation of lighting effects; and

19  
20 comparing the two dimensional image with each of the  
21 rendered three dimensional candidate models.

1 27. A computer program product embodied in a computer-  
2 readable medium for matching a two dimensional image to one of a  
3 plurality of three dimensional candidate models stored in a  
4 database, the computer program product comprising:

5  
6 computer readable program code means for determining  
7 the position and orientation of an object giving rise to the two  
8 dimensional image;

9  
10 computer readable program code means for computing a  
11 representation of lighting effects based on the plurality of  
12 three dimensional candidate models and the two dimensional image  
13 that allows evaluation of the likelihood that a particular three  
14 dimensional candidate model gave rise to a particular two  
15 dimensional image; and

16  
17 computer readable program code means for choosing the  
18 most likely three dimensional candidate model to have generated  
19 the query based on the computed representation of lighting  
20 effects.

1 28. A program storage device readable by machine, tangibly  
2 embodying a program of instructions executable by the machine to  
3 perform method steps for matching a two dimensional image to one  
4 of a plurality of three dimensional candidate models, the method  
5 comprising the steps of:  
6

7           determining the position and orientation of an object  
8 giving rise to the two dimensional image;

9  
10           computer readable program code means for computing a  
11 representation of lighting effects based on the plurality of  
12 three dimensional candidate models and the two dimensional image  
13 that allows evaluation of the likelihood that a particular three  
14 dimensional candidate model gave rise to a particular two  
15 dimensional image; and

16  
17           computer readable program code means for choosing the  
18 most likely three dimensional candidate model to have generated  
19 the query based on the computed representation of lighting  
20 effects.

**METHOD FOR MATCHING A TWO DIMENSIONAL IMAGE TO ONE OF A PLURALITY  
OF THREE DIMENSIONAL CANDIDATE MODELS CONTAINED IN A DATABASE**

ABSTRACT OF THE DISCLOSURE

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A method for matching a two dimensional image to one of a plurality of three dimensional candidate models. The method including the steps of: determining the position and orientation of the two dimensional image; for each three dimensional model, computing a histogram-like table having a computed brightness coefficient for each surface normal of the model based on the corresponding value in the two dimensional image, each brightness coefficient depending only on the corresponding surface normal; and either successively rendering each three dimensional model in the determined position and orientation using the surface normals in conjunction with the corresponding computed brightness histogram-like table; and comparing the two dimensional image with each of the rendered three dimensional models or computing the variance of the brightness coefficients that are used to create each bucket of the histogram-like table, a bucket being a set of similar normal values that are lumped together to form a single argument value in the histogram-like table; computing the sum of the variances of the histogram-like table buckets; and ranking the three dimensional models using its computed sum as an error function, the ranking indicating the likelihood that the corresponding three dimensional model matches the two dimensional image. Also provided is a program storage device readable by machine, tangibly embodying a program of instructions executable by the machine to perform the method steps of the present invention and a computer program product embodied in a computer-readable medium for carrying out the methods of the present invention.

Fig. 1

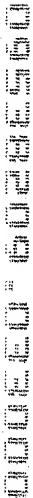




Fig. 2

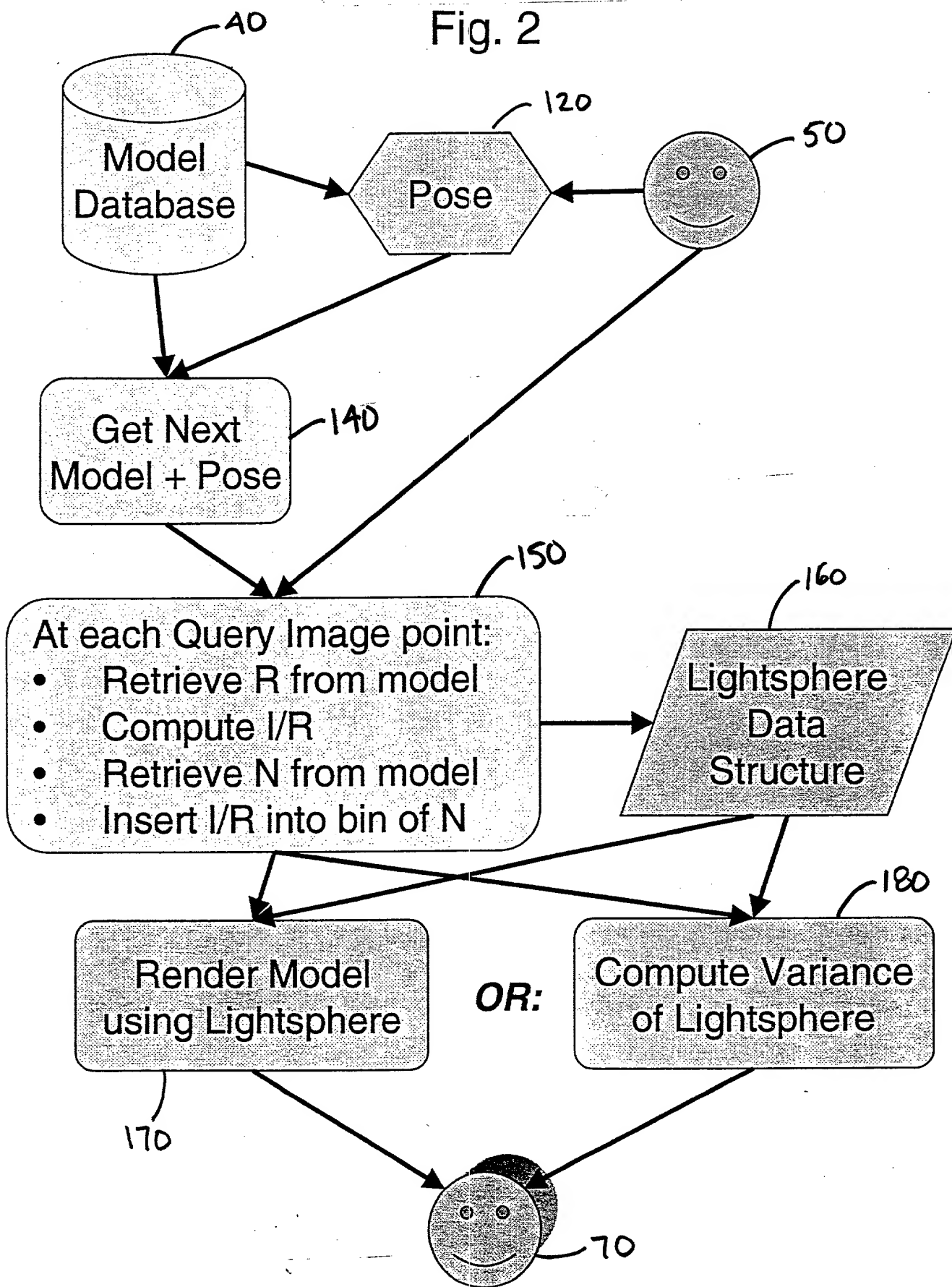
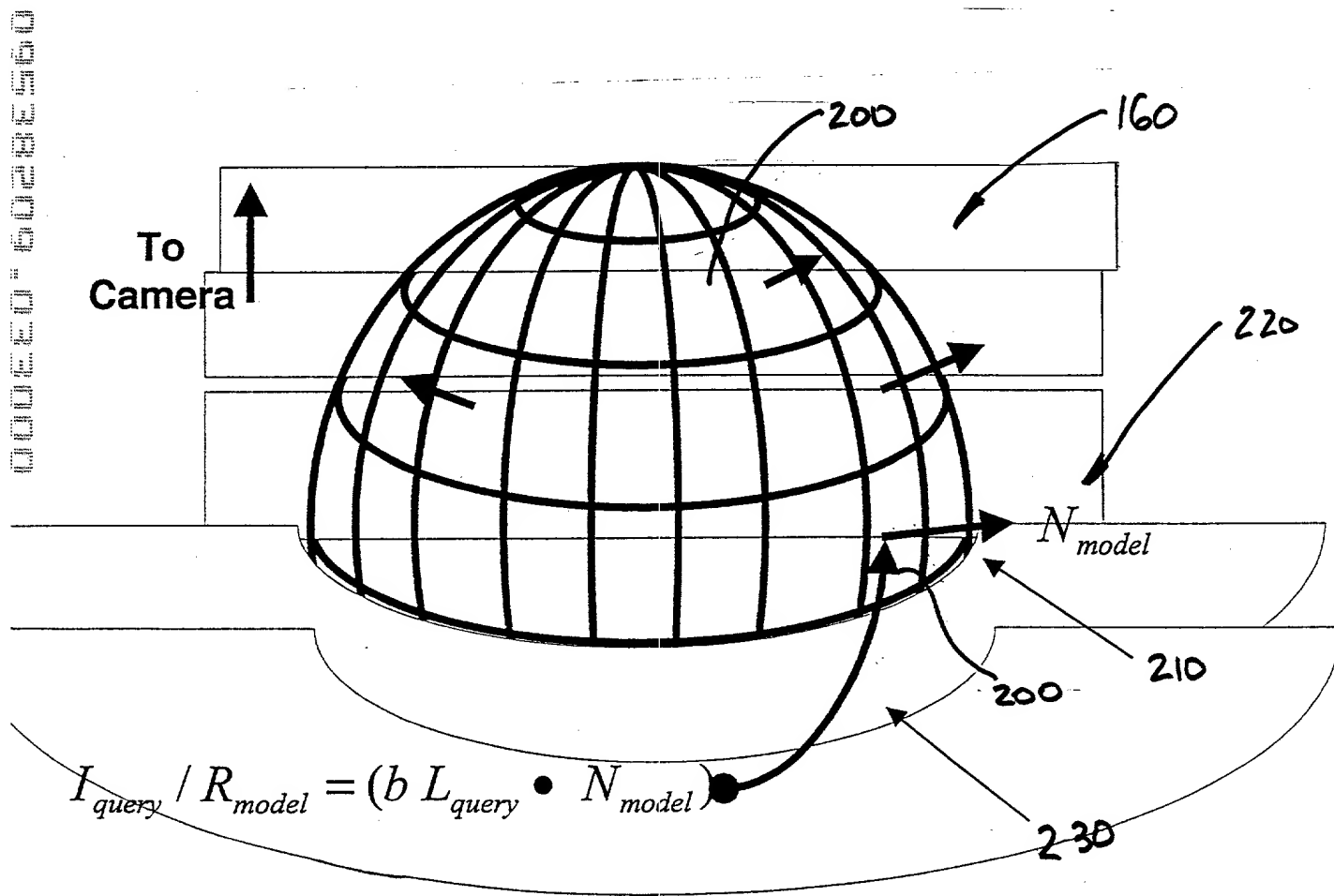


Fig. 3



Docket No.  
13414 (NECI1083)

# Declaration and Power of Attorney For Patent Application

## English Language Declaration

As a below named inventor, I hereby declare that:

My residence, post office address and citizenship are as stated below next to my name,

I believe I am the original, first and sole inventor (if only one name is listed below) or an original, first and joint inventor (if plural names are listed below) of the subject matter which is claimed and for which a patent is sought on the invention entitled

### METHOD FOR MATCHING A TWO DIMENSIONAL IMAGE TO ONE OF A PLURALITY OF THREE DIMENSIONAL CANDIDATE MODELS CONTAINED IN A DATABASE

the specification of which

(check one)

☒ is attached hereto.

☐ was filed on \_\_\_\_\_ as United States Application No. or PCT International Application Number \_\_\_\_\_ and was amended on \_\_\_\_\_ (if applicable)

I hereby state that I have reviewed and understand the contents of the above identified specification, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose to the United States Patent and Trademark Office all information known to me to be material to patentability as defined in Title 37, Code of Federal Regulations, Section 1.56.

I hereby claim foreign priority benefits under Title 35, United States Code, Section 119(a)-(d) or Section 365(b) of any foreign application(s) for patent or inventor's certificate, or Section 365(a) of any PCT International application which designated at least one country other than the United States, listed below and have also identified below, by checking the box, any foreign application for patent or inventor's certificate or PCT International application having a filing date before that of the application on which priority is claimed.

Prior Foreign Application(s)

Priority Not Claimed

(Number)

(Country)

(Day/Month/Year Filed)

☐

(Number)

(Country)

(Day/Month/Year Filed)

☐

(Number)

(Country)

(Day/Month/Year Filed)

☐

I hereby claim the benefit under 35 U.S.C. Section 119(e) of any United States provisional

\_\_\_\_\_  
(Application Serial No.)

\_\_\_\_\_  
(Filing Date)

\_\_\_\_\_  
(Application Serial No.)

\_\_\_\_\_  
(Filing Date)

\_\_\_\_\_  
(Application Serial No.)

\_\_\_\_\_  
(Filing Date)

I hereby claim the benefit under 35 U. S. C. Section 120 of any United States application(s), or Section 365(c) of any PCT International application designating the United States, listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States or PCT International application in the manner provided by the first paragraph of 35 U.S.C. Section 112, I acknowledge the duty to disclose to the United States Patent and Trademark Office all information known to me to be material to patentability as defined in Title 37, C. F. R., Section 1.56 which became available between the filing date of the prior application and the national or PCT International filing date of this application:

\_\_\_\_\_  
(Application Serial No.)

\_\_\_\_\_  
(Filing Date)

\_\_\_\_\_  
(Status)  
(patented, pending, abandoned)

\_\_\_\_\_  
(Application Serial No.)

\_\_\_\_\_  
(Filing Date)

\_\_\_\_\_  
(Status)  
(patented, pending, abandoned)

\_\_\_\_\_  
(Application Serial No.)

\_\_\_\_\_  
(Filing Date)

\_\_\_\_\_  
(Status)  
(patented, pending, abandoned)

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

POWER OF ATTORNEY: As a named inventor, I hereby appoint the following attorney(s) and/or agent(s) to prosecute this application and transact all business in the Patent and Trademark Office connected therewith. *(list name and registration number)*

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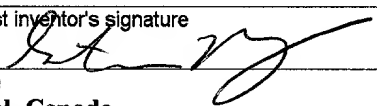
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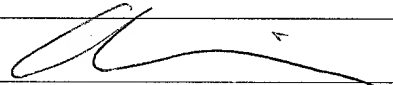
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